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## NATIONAL INSTITUTE OF TECHNOLOGY HAMIRPUR <br> Department of Mathematics \& Scientific Computing <br> End-semester examination <br> Class: B. Tech $-6^{\text {th }}$ Semester

Course Title: Time series Analysis
Maximum Marks: 50


Note: All questions are compulsory and carry equal marks (5).

Course code: MA -323
Time: 3:00 Hours
Q. 1 a) Define Stationary and non-stationary time series. Check the stationarity of the following model.

$$
z_{t}-z_{t-1}=a_{t}-1.3 a_{t-1}+0.3 a_{t-2}
$$

b) Write the operator form of the following models.

$$
z_{t}-0.5 z_{t-1}=a_{t}-1.3 a_{t-1}+0.4 a_{t-2}
$$

Q. 2 Define ARIMA models and also discuss Box-jenkins methodology.
Q. 3 Discuss mean, variance and autocorrelation function of autoregressive $\operatorname{AR}(2)$ and moving average MA (2).
Q. 4 a) For AR (2) process, $\quad z_{t}=1.0 z_{t-1}+0.5 z_{t-2}+a_{t}$

Calculate mean, variance, auto-correlation function of $z_{t}$.
b) Evaluate the mean, variance and autocorrelation function of $z_{t}=a_{t}+1.3 a_{t-1}+0.4 a_{t-2}$
Q. 5 What are exponential smoothing methods? Explain Simple exponential smoothing method and Holt's trend corrected method along with procedure.
Q. 6 Calculate the forcaste values for the given weekly demand values by using Holt's trend corrected method by taking smoothing parameters $\alpha=0.2$ and $\beta=0.1$.

| Week | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Actual demand | 210 | 198 | 195 | 204 | 217 | 229 | 207 | 214 | 209 | 223 |

Q. 7 Compute the seasonal indices by using ratio to trend method, from the following data

| Year | Quarter -I | Quarter -II | Quarter -III | Quarter -IV |
| :---: | :---: | :---: | :---: | :---: |
| 2000 | 32 | 38 | 36 | 34 |
| 2001 | 42 | 52 | 38 | 42 |
| 2002 | 52 | 50 | 42 | 52 |
| 2003 | 62 | 68 | 56 | 74 |
| 2005 | 80 | 88 | 82 | 90 |


Q. 8 a) Find the cross correlation and covariance matrix for the given data set.

| Time | Variable 1 | Variable 2 |
| :---: | :---: | :---: |
| $\mathbf{1}$ | 20 | 30 |
| $\mathbf{2}$ | 21 | 31 |

b) Write the mathematical formulation of VARMA ( $\mathrm{p}, \mathrm{q}$ ) and what is the condition for stable?
Q. 9 a) What is multivariate time series? What are the conditions for stationary multivariate time series.
b) What is the difference between correlation and covariance?
Q. 10 Discuss the SARIMA models and classify as a member of the class of ARIMA (p, d, q) processes in the following model

$$
(1-0.2 \mathrm{~B})(1-\mathrm{B}) z_{t}=(1-0.5 \mathrm{~B}) a_{t}
$$

