

**National Institute of Technology, Hamirpur (H.P.)**

**M. Tech. Mechanical Engineering (Design)**

**End-Semester Examination (Session 2020-21)**

**Branch:** M.tec (Design Engineering)

**Course Name:** Adv. Mech. of Solids

**Time Allowed:** 2 hours

**Date:** 14-12-2020

**Semester:** Ist

**Course Code:** ME-631

**Maximum Marks:** 50

**Time Slot:** 15:00-17:00 Hrs

**Instruction to candidates:**

- Attempt all the questions in the order as appear in the question paper.
- Marks are indicated against each question.
- Assume if there is any missing data with little explanation
- **Keep your web-cameras on for invigilation purpose**

Q1. Write short notes on:

**(5x2=10)**

(a) State of stress at a point (b) Airy's Stress Function (c) Compatibility Conditions (d) Torsion of Prismatic shafts (e) Fictitious Load method

Q2. The known stress components at a point in a body, relative to the (x, y, z) axes, are  $\sigma_{xx} = 20$  MPa,  $\sigma_{yy} = 10$  MPa,  $\sigma_{xy} = 30$  MPa,  $\sigma_{xz} = -10$  MPa, and  $\sigma_{yz} = 80$  MPa. Also, the second stress invariant is  $I_2 = -7800$  (MPa)<sup>2</sup>

(a) Determine the stress component  $\sigma_{zz}$ . Then determine the stress invariants  $I_1$ , and  $I_3$ , and the three principal stresses.

(b) Show that  $I_1$ ,  $I_2$  and  $I_3$ , are the same relative to (x, y, z) axes and relative to principal axes (1, 2, 3). **(10)**

Q3. The rectangular components of small strain at a point is given by the following matrix. Determine the principal strain and the direction of the maximum unit strain. **(10)**

$$[\varepsilon_{ij}] = p \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -4 \\ 0 & -4 & 3 \end{bmatrix} \text{ where } p = 10^{-4}$$

Q4. (a) Explain the yield surfaces of Tresca and Von-mises. **(5)**

(b) Determine the diameter of a ductile steel bar if the tensile load  $F$  is 35,000 N and the torsional moment  $T$  is 1800 Nm. Use a factor of safety of 1.5. Take  $E = 207 \times 10^6$  kPa and  $\sigma_{yp} = 207,000$  kPa. Use suitable theory of Failure. **(5)**

Q5. A thin walled circular ring is loaded as shown in the figure. Determine the vertical displacement of Point A, only considering the bending energy. **(10)**

